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2 pages

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Indexed by

A3278
→ AG997
- A7001
A3107

Jim, back in 1991 you very kindly suggested,
(among other things) the following:

[with some comments, or rather requests!, from me in square brackets]

I think the sequence
1,2,4,5,10,11,13,14,...

[yes , it is there, sequence A3278]

should be included, with a reference to Erdős and Turán's
"On some sequences of Integers" (J. London Math. Soc. 11 (1936),
261-264). I also suggest the related sequences
0,0,1,0,0,1,1,2,2,0,0,1,0,0,1,1,2,2,1,2,2,3,3,4,3,3,4, ...
1,2,4,6,8,12,14, ...
1,2,4,7,11,17,36, ...

studied by Joseph Gerver, Jamie Simpson, and myself in "Greedy
Partitioning the Natural Numbers into Sets Free of Arithmetic
Progressions" (Proc. AMS, 102 (1988), 765-772). All three can
be described as self-generating sequences; I can send you more
terms if you like.

← Mira,
get from library
please

[no, i don't have these, and i would like to!
can you send more terms? a copy of the paper?
they will be sequences A6997 - A6999]

I think sequence 37 should be labelled "representations as a sum
of *distinct* Fibonacci numbers"; representations as a sum of
(not necessarily distinct) Fibonacci numbers are enumerated by
the sequence
1,2,3,3,6,9, ...
(not included in the first edition).

I don't get this either way

[do you happen to have more terms of this one? sorry, but i have
a zillion of these sequences to extend and enter!
this one will be A7000]

$(1-x)(1-x^2)(1-x^3)$ gives A3107

The self-generating sequence
1,2,1,2,3,1,2,1,2,3,1,2,3,4, ...
(not in the first edition) is related to the Catalan numbers as
1,2,1,2,2,1,2,1,2,2,1,2,2, ...
(sequence 36) is related to the Fibonacci numbers; I think it
might be worth including.

$(1-x)^2(1-x^2)(1-x^3)(1-x^5)$... gives

1, 2, 4, 7, 11, ...

[what is the defn? This will be A7001]

new,
Call it
A7000
to Mira, please
enter
see next
page

index

The sequence $S(n)$ with terms given by

1, 2, 3, 6, 7, 8, 9, 12, 15, 18, ...

the unique sequence with the property that $S(1)=1$ and $S(S(n))=3n$ for all n . (I published a problem on this in Crux Mathematicorum a long time ago; unfortunately, I don't have the reference handy.)

unclear

[Jim, i can't make any sense out of that one, which sounds very intriguing. You can't mean $S(S(n))=3n$??]

Best regards
Neil

*I think he means
 $S(S(S(n))) = 3n$*

for $n \geq 4$

*but it still
is wrong*

~~*$S(S(S(n))) = 3n$*~~

~~*$S(S(S(n))) = 3n$*~~

~~*$S(S(S(n))) = 3n - 2$*~~